

Goniometrické vzorce

- $\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta,$
- $\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta,$
- $\sin 2\alpha = 2 \sin \alpha \cos \alpha, \quad \cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha, \quad \cos^2 \alpha + \sin^2 \alpha = 1,$
- $\cos^2 \alpha = \frac{1 + \cos 2\alpha}{2}, \quad \sin^2 \alpha = \frac{1 - \cos 2\alpha}{2},$
- $\cos \alpha \cos \beta = \frac{1}{2} (\cos(\alpha + \beta) + \cos(\alpha - \beta)),$
- $\sin \alpha \sin \beta = \frac{1}{2} (\cos(\alpha - \beta) - \cos(\alpha + \beta)),$
- $\sin \alpha \cos \beta = \frac{1}{2} (\sin(\alpha - \beta) + \sin(\alpha + \beta)).$
- $\sin 0 = \cos \frac{\pi}{2} = \frac{\sqrt{0}}{2}, \quad \sin \frac{\pi}{6} = \cos \frac{\pi}{3} = \frac{\sqrt{1}}{2}, \quad \sin \frac{\pi}{4} = \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2},$
- $\sin \frac{\pi}{3} = \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2}, \quad \sin \frac{\pi}{2} = \cos 0 = \frac{\sqrt{4}}{2},$
- $\cos n\pi = (-1)^n, \quad \sin(2k-1)\frac{\pi}{2} = (-1)^{k+1}, \quad \cos(2k-1)\frac{\pi}{2} = 0,$

Integrály

- $\int e^{\alpha x} \cos \beta x \, dx = \frac{e^{\alpha x}}{\alpha^2 + \beta^2} (\alpha \cos \beta x + \beta \sin \beta x),$
- $\int e^{\alpha x} \sin \beta x \, dx = \frac{e^{\alpha x}}{\alpha^2 + \beta^2} (\alpha \sin \beta x - \beta \cos \beta x),$

Substitúcie

- $\operatorname{tg} \frac{x}{2} = t, \quad x = 2 \operatorname{arctg} t, \quad dx = \frac{2dx}{1+t^2}, \quad \sin x = \frac{2t}{t^2+1}, \quad \cos x = \frac{1-t^2}{t^2+1},$
- $\operatorname{tg} x = t, \quad x = \operatorname{arctg} t, \quad dx = \frac{dx}{1+t^2}, \quad \sin^2 x = \frac{t^2}{t^2+1}, \quad \cos^2 x = \frac{1}{t^2+1}, \quad \sin 2x = \frac{2t}{t^2+1},$
- $\sqrt[k]{\frac{ax+b}{cx+d}} = t, \quad \frac{ax+b}{cx+d} = t^k, \quad x = ?, \quad dx = ?,$
- $a > 0, \quad \sqrt{ax^2 + bx + c} = \sqrt{a}x \pm t, \quad ax^2 + bx + c = ax^2 \pm 2\sqrt{a}xt + t^2, \quad x = ?, \quad dx = ? \quad \sqrt{ax^2 + bx + c} = ?$
- $c > 0, \quad \sqrt{ax^2 + bx + c} = \sqrt{c} \pm xt, \quad ax^2 + bx + c = c \pm 2\sqrt{c}xt + x^2t^2, \quad x = ?, \quad dx = ? \quad \sqrt{ax^2 + bx + c} = ?$
- $x = \varrho \cos \varphi, \quad y = \varrho \sin \varphi, \quad J_g(\varrho, \varphi) = \varrho,$
- $x = \varrho \cos \varphi, \quad y = \varrho \sin \varphi, \quad z = u, \quad J_g(\varrho, \varphi, u) = \varrho,$
- $x = \varrho \cos \varphi \cos \vartheta, \quad y = \varrho \sin \varphi \cos \vartheta, \quad z = \varrho \sin \vartheta, \quad J_g(\varrho, \varphi, \vartheta) = \varrho^2 \cos \vartheta.$