

1. Komplexné číslo c napíšte v algebraickom tvare, znázornite v komplexnej rovine a vypočítajte absolútnu hodnotu $|c|$
 - a. $c = \frac{1}{2+i}$ [$c = \frac{2}{3} - \frac{1}{3}i$, $|c| = \frac{\sqrt{5}}{5}$]
 - b. $c = \frac{(2-3i)(1+2i)}{2+i}$ [$z = \frac{17}{5} - \frac{6}{5}i$, $|c| = \sqrt{13}$]
 - c. $c = \left(\frac{1+i}{1-i}\right)^4$ [$c = 1 = |c|$]
2. Riešte kvadratické rovnice
 - a. $3x^2 + x - 2 = 0$ [$\{-1; \frac{2}{3}\}$]
 - b. $2x^2 - 2x + 1 = 0$ [$\frac{1}{2} \pm \frac{1}{2}i$]
 - c. $2x^2 - 2x + 5 = 0$ [$\frac{1}{2} \pm \frac{3}{2}i$]
3. Riešte rovnice
 - a. $(1+i)x = 2 - 3i$ [$-\frac{1}{2} - \frac{5}{2}i$]
 - b. $x - 2ix + 1 - 2i = 1$ [$-\frac{4}{5} + \frac{2}{5}i$]
 - c. $3x + 2ix + 1 - 3i = x + ix - 1$ [$-\frac{1}{5} + \frac{8}{5}i$]
4. Nájdite reálne čísla x, y , ktoré spĺňajú rovnice:
 - a. $x(2+3i) + y(4-5i) = 6 - 2i$ [$x = y = 1$]
 - b. $(x-i)(2-yi) = 11 - 23i$ [(7, 3); (-3/2, -14)]
 - c. $\frac{x}{2+3i} + \frac{y}{3+2i} = 1$ [(-26/5, 39/5)]
5. V obore komplexných čísel riešte rovnice
 - a. $z^2 + 3\bar{z} = 0$ [$z_1 = 0$, $z_2 = -3$, $z_{3,4} = \frac{3}{2} \pm i\sqrt{3}\frac{3}{2}$,]
 - b. $2z + (1+i)\bar{z} = 1 - 3i$ [$z = 2 - 5i$]
 - c. $\frac{z+1}{\bar{z}-1} = -1$ [$\{iy: y \in \mathbb{R}\}$]
6. Určte goniometrický tvar a znázornite v komplexnej rovine čísla
 $3, -3, 3i, -3i, 1+i, -1-i, \sqrt{3}+i, -1+i\sqrt{3}$
 $[3 = 3(\cos 0 + i \sin 0), -3 = 3(\cos \pi + i \sin \pi), 3i = 3(\cos \frac{\pi}{2} + i \sin \frac{\pi}{2}), -3i = 3(\cos \frac{3\pi}{2} + i \sin \frac{3\pi}{2}),$
 $1+i = \sqrt{2}(\cos \frac{\pi}{4} + i \sin \frac{\pi}{4}), -1-i = \sqrt{2}(\cos \frac{5\pi}{4} + i \sin \frac{5\pi}{4}), \sqrt{3}+i = 2(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6}),$
 $-1+i\sqrt{3} = 2(\cos \frac{2\pi}{3} + i \sin \frac{2\pi}{3})]$
7. Riešte binomické rovnice. Riešenie vyjadrite v goniometrickom aj algebraickom tvare a znázornite.
 - a. $z^3 = -8i$, b. $z^3 = 8i$, c. $z^4 = -4$, d. $z^4 = -1 + i\sqrt{3}$,
 - e. $z^4 = -1 - i\sqrt{3}$, f. $z^6 = -8$, g. $z^6 = 1$
 - [a. $z_k = 2(\cos(\frac{\pi}{2} + k\frac{2\pi}{3}) + i \sin(\frac{\pi}{2} + k\frac{2\pi}{3}))$, $k = 0, 1, 2$;
 - b. $z_k = 2(\cos(\frac{\pi}{6} + k\frac{2\pi}{3}) + i \sin(\frac{\pi}{6} + k\frac{2\pi}{3}))$, $k = 0, 1, 2$;
 - c. $z_k = \sqrt{2}(\cos(\frac{\pi}{4} + k\frac{\pi}{2}) + i \sin(\frac{\pi}{4} + k\frac{\pi}{2}))$, $k = 0, 1, 2, 3$;
 - d. $z_k = \sqrt[4]{2}(\cos(\frac{\pi}{6} + k\frac{\pi}{2}) + i \sin(\frac{\pi}{6} + k\frac{\pi}{2}))$, $k = 0, 1, 2, 3$
 - e. $z_k = \sqrt[4]{2}(\cos(\frac{\pi}{3} + k\frac{\pi}{2}) + i \sin(\frac{\pi}{3} + k\frac{\pi}{2}))$, $k = 0, 1, 2, 3$
 - f. $z_k = \sqrt{2}(\cos(\frac{\pi}{6} + k\frac{\pi}{3}) + i \sin(\frac{\pi}{6} + k\frac{\pi}{3}))$, $k = 0, 1, 2, 3, 4, 5$
 - g. $z_k = (\cos(\frac{\pi}{3} + k\frac{\pi}{3}) + i \sin(\frac{\pi}{3} + k\frac{\pi}{3}))$, $k = 0, 1, 2, 3, 4, 5]$